

Name: _____ Date: _____
 A2CC: Arithmetic Sequences

1) Find the next two terms of each sequence. Then describe the pattern. The equations will be completed later.

1, 3, 5, 7, 9, _____, _____ Description: _____ Equation: _____

2, 7, 12, 17, 22, _____, _____ Description: _____ Equation: _____

-416, -323, -230, -137, _____, _____ Description: _____ Equation: _____

-2, -5, -8, -11, _____, _____ Description: _____ Equation: _____

2) So we take the **1st term**, and keep adding the _____ over and over again. This is the definition of an **arithmetic sequence**.

3) **(the n th term) = (the 1st term) + (the common difference)($n - 1$)**

4) In other words... $a_n = a_1 + d(n - 1)$

 5) Examine the following sequence: 2, 7, 12, 17, 22, ...

a] What is the **1st term**?

b] What is the **common difference**?

c] What is the 35th term?

d] What is the formula to find the **n th** term?

6) Examine the following sequence: 100, 90, 80, 70, 60, ...

a] What is the **1st term**?

b] What is the **common difference**?

c] What is the 28th term?

d] What is the formula to find the **nth** term?

***So the **common difference** can be positive OR negative!!!

7) How many terms are in the sequence: 7, 10, 13, ..., 55 ?

8) Insert 3 arithmetic means between 7 and 23.

SUM OF AN ARITHMETIC SERIES

Given an arithmetic series with n terms, $\{a_1, a_2, \dots, a_n\}$, then its sum is given by:

$$S_n = \frac{n}{2}(a_1 + a_n)$$

9) Which of the following is the sum of the first 100 natural numbers? Show the process that leads to your choice.

- | | |
|-----------|------------|
| (1) 5,000 | (3) 10,000 |
| (2) 5,100 | (4) 5,050 |

10) Find the sum of each arithmetic series described or shown below.

(a) The sum of the sixteen terms given by:

$$-10 + -6 + -2 + \dots + 46 + 50.$$

(b) The first term is -8 , the common difference, d , is 6 and there are 20 terms

(c) The last term is $a_{12} = -29$ and the common difference, d , is -3 .

(d) The sum $5 + 8 + 11 + \dots + 77$.

- 11) Kirk has set up a college savings account for his son, Maxwell. If Kirk deposits \$100 per month in an account, increasing the amount he deposits by \$10 per month each month, then how much will be in the account after 10 years?

5. For an arithmetic series that sums to 1,485, it is known that the first term equals 6 and the last term equals 93. *Algebraically* determine the number of terms summed in this series.

APPLICATIONS

6. Arlington High School recently installed a new black-box theatre for local productions. They only had room for 14 rows of seats, where the number of seats in each row constitutes an arithmetic sequence starting with eight seats and increasing by two seats per row thereafter. How many seats are in the new black-box theatre? Show the calculations that lead to your answer.
7. Simeon starts a retirement account where he will place \$50 into the account on the first month and increasing his deposit by \$5 per month each month after. If he saves this way for the next 20 years, how much will the account contain in principal?
8. The distance an object falls per second while only under the influence of gravity forms an arithmetic sequence with it falling 16 feet in the first second, 48 feet in the second, 80 feet in the third, etcetera. What is the total distance an object will fall in 10 seconds? Show the work that leads to your answer.
9. A large grandfather clock strikes its bell once at 1:00, twice at 2:00, three times at 3:00, etcetera. What is the total number of times the bell will be struck in a day? Use an arithmetic series to help solve the problem and show how you arrived at your answer.
- 10) Examine the following sequence: 3, 7, 11, 15, 19, ...
- a] What is the **1st term**?
- b] What is the **common difference**?

c] What is the 13th term?

d] What is the formula to find the **nth** term?

11) Examine the sequence: 111, 99, 87, 75, 63, ...

a] What is the **1st term**?

b] What is the **common difference**?

c] What is the 40th term?

d] What is the formula to find the **nth** term?

12) Find the 311th term in the sequence: 7, 25, 43, 61, ...

13) Find the 90th term in the sequence: 100, 97, 94, 91, ...

